



# Production de puissance



**NRJ EN ROTATION**

# Problème

Une turbine à gaz opère avec 2 compresseurs et un régénérateur. Les paramètres de l'air à l'entrée du système sont  $p_1 = 101.3 \text{ kPa}$  et  $T_1 = 290 \text{ K}$ , la température à l'entrée de la turbine est  $T_3 = 973 \text{ K}$ . Le rapport de compression total est  $r_p = 5$ ,  $\gamma = 1.4$ ,  $c_p = 1005 \text{ J/kg K}$ . Calculer le rendement de l'installation si: a)  $\eta_C = 1 = \eta_T, \sigma = 0.7$  b)  $\eta_C = 0.85 = \eta_T, \sigma = 0.7$

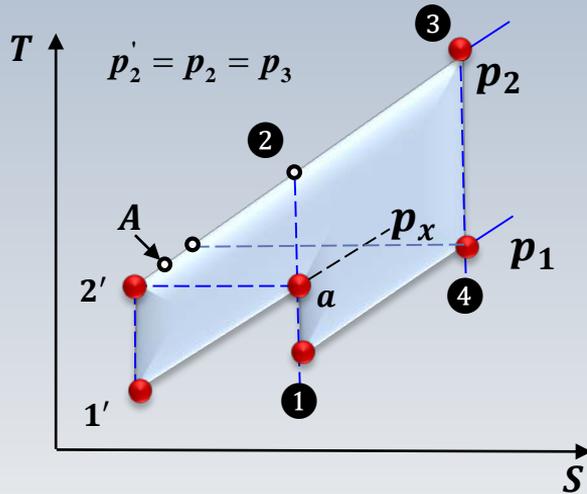
Ce problème sera d'abord regardé étape par étape et par la suite, au moyen d'une formule abrégée

# Problème

$$p_1 = 101.3 \text{ kPa}, T_1 = 290 \text{ K}, T_3 = 973 \text{ K}$$

$$r_p = 5, \gamma = 1.4, c_p = 1005 \text{ J/kg} \cdot \text{K}$$

$$a) \eta_c = 1 = \eta_T, \sigma = 0.7$$



Pression intermédiaire  $p_x$  (optimisée)

$$p_x = \sqrt{p_1 p_2} = \sqrt{5 p_1^2} = 2.236 p_1$$

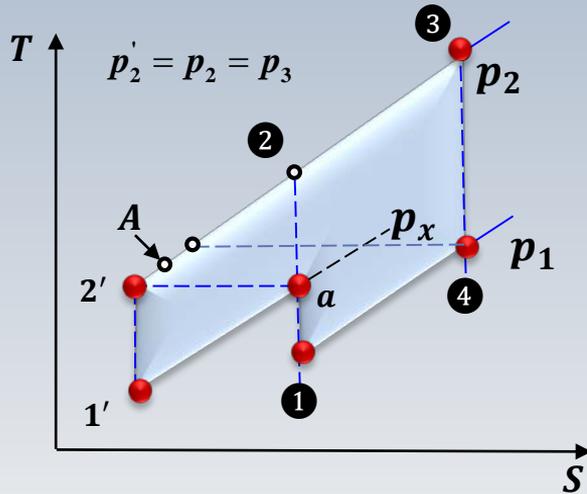
$$\Delta = \left( \frac{p_2}{p_1} \right)^{\frac{\gamma-1}{\gamma}} = (5)^{\frac{1.4-1}{1.4}} = 1.5838$$

Compression 1-a

$$\Delta^* = \left( \frac{p_x}{p_1} \right)^{\frac{\gamma-1}{\gamma}} = (2.236)^{\frac{0.4}{1.4}} = 1.2584$$

# Problème

$p_1 = 101.3 \text{ kPa}$ ,  $T_1 = 290 \text{ K}$ ,  $T_3 = 973 \text{ K}$   
 $r_p = 5$ ,  $\gamma = 1.4$ ,  $c_p = 1005 \text{ J/kg} \cdot \text{K}$   
a)  $\eta_C = 1 = \eta_T$ ,  $\sigma = 0.7$



$$T_a = T_1 \left( \frac{p_x}{p_1} \right)^{\frac{\gamma-1}{\gamma}} = T_1 \Delta^*$$
$$= 290 \times 1.2584 = \mathbf{365 \text{ K}}$$

$$W_C = c_p (T_a - T_1) + c_p (T_{2'} - T_{1'})$$
$$(T_{1'} = T_1, \quad T_{2'} = T_a)$$

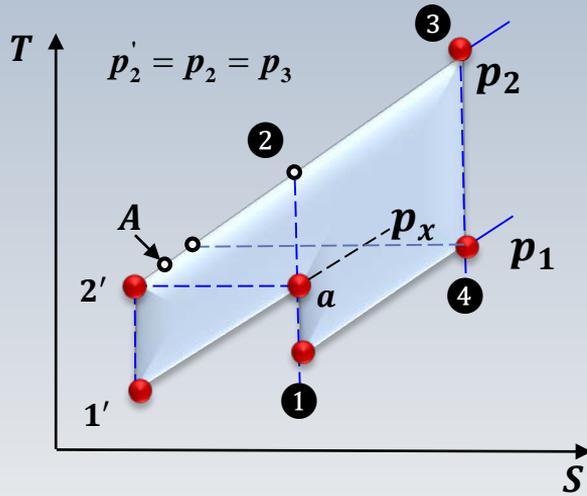
$$W_C = 2c_p T_1 (\Delta^* - 1)$$
$$= 2 \times 1.005 \times 290 \times (1.2584 - 1)$$
$$= \mathbf{150.6 \text{ (kJ/kg)}}$$

# Problème

$$p_1 = 101.3 \text{ kPa}, T_1 = 290 \text{ K}, T_3 = 973 \text{ K}$$

$$r_p = 5, \gamma = 1.4, c_p = 1005 \text{ J/kg} \cdot \text{K}$$

$$a) \eta_c = 1 = \eta_T, \sigma = 0.7$$



$$\Delta = \left( \frac{p_2}{p_1} \right)^{\frac{\gamma-1}{\gamma}} = \left( \frac{T_2}{T_1} \right) = \left( \frac{T_3}{T_4} \right)$$

$$= 1.5838$$

Travail produit par la turbine

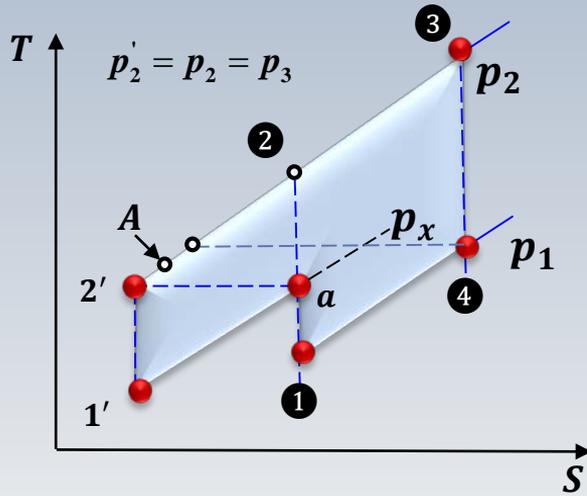
$$W_T = c_p (T_3 - T_4) = c_p T_3 \left( 1 - \frac{1}{\Delta} \right)$$

$$W_T = 1.005 \times 973 \times \left( 1 - \frac{1}{1.5838} \right)$$

$$= 360.4 \text{ (KJ/kg)}$$

# Problème

$$p_1 = 101.3 \text{ kPa}, T_1 = 290 \text{ K}, T_3 = 973 \text{ K}$$
$$r_p = 5, \gamma = 1.4, c_p = 1005 \text{ J/kg} \cdot \text{K}$$
$$a) \eta_c = 1 = \eta_T, \sigma = 0.7$$



Chaleur fournie  $(\Delta = 1.5838)$

$$T_4 = T_3 / \Delta = 973 / 1.5838 = 614.3 \text{ K}$$

point A

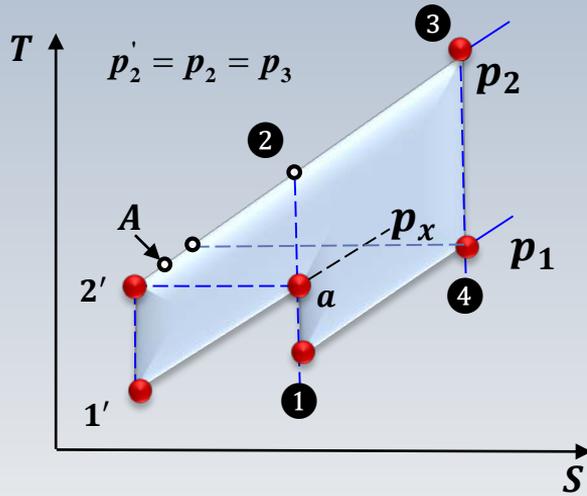
$$T'_2 = T_a = 365 \text{ K}$$

$$T_A = T'_2 + \sigma(T_4 - T'_2)$$
$$= 365 + 0.7(614.3 - 365) = 539.5 \text{ K}$$

$$Q = c_p(T_3 - T_A) = 1.005(973 - 539.5)$$
$$= 435.6 \text{ kJ/kg}$$

# Problème

$p_1 = 101.3 \text{ kPa}$ ,  $T_1 = 290 \text{ K}$ ,  $T_3 = 973 \text{ K}$   
 $r_p = 5$ ,  $\gamma = 1.4$ ,  $c_p = 1005 \text{ J/kg} \cdot \text{K}$   
a)  $\eta_c = 1 = \eta_T$ ,  $\sigma = 0.7$



Le rendement

$$\eta = \frac{W_T - W_C}{Q}$$

$$W_T = 360.4 \text{ (KJ/kg)}$$

$$W_C = 150.6 \text{ (kJ/kg)}$$

$$Q = 435.6 \text{ kJ/kg}$$

$$\eta = 0.482$$



# Formule abrégée

$p_1 = 101.3 \text{ kPa}$ ,  $T_1 = 290 \text{ K}$ ,  $T_3 = 973 \text{ K}$   
 $r_p = 5$ ,  $\gamma = 1.4$ ,  $c_p = 1005 \text{ J/kg} \cdot \text{K}$   
a)  $\eta_c = 1 = \eta_T$ ,  $\sigma = 0.7$

$$\eta = \frac{\frac{\Delta - 1}{\Delta} \Phi \eta_T - \frac{2(\sqrt{\Delta} - 1)}{\eta_c}}{\frac{\Delta - 1}{\Delta} \sigma \Phi \eta_T + (1 - \sigma) \left[ \Phi - 1 - \frac{\sqrt{\Delta} - 1}{\eta_c} \right]}$$

$$\Delta = \left( \frac{p_2}{p_1} \right)^{\gamma-1/\gamma} = 1.5838$$
$$\Phi = \left( \frac{T_3}{T_1} \right) = \left( \frac{973}{290} \right) = 3.35$$
$$\eta_c = \eta_T = 1, \quad \sigma = 0.7$$

$$\eta = \frac{\frac{1.5838 - 1}{1.5838} \times 3.35 \times 1 - \frac{2(\sqrt{1.5838} - 1)}{1}}{\frac{1.5838 - 1}{1.5838} \times 0.7 \times 3.35 \times 1 + (1 - 0.7) \left[ 3.35 - 1 - \frac{\sqrt{1.5838} - 1}{1} \right]} = 0.482$$



# Problème

$$p_1 = 101.3 \text{ kPa}, T_1 = 290 \text{ K}, T_3 = 973 \text{ K}$$
$$r_p = 5, \gamma = 1.4, c_p = 1005 \text{ J/kg} \cdot \text{K}$$
$$b) \eta_c = 0.85 = \eta_T, \sigma = 0.7$$

$$W_{Ts} = 360.4 \text{ (kJ/kg)}$$

$$W_{Cs} = 150.6 \text{ (kJ/kg)}$$

$$\Delta = \left( \frac{p_2}{p_1} \right)^{\gamma-1/\gamma} = 1.5838, \quad \Phi = \left( \frac{T_3}{T_1} \right) = \left( \frac{973}{290} \right) = 3.35$$

$$W_C = 150.6/0.85 = 177.2 \text{ (kJ/kg)}$$

$$W_T = 0.85(360.4) = 306.3 \text{ (kJ/kg)}$$

$$\eta = \frac{\frac{1.5838-1}{1.5838} \times 3.35 \times 0.85 - \frac{2(\sqrt{1.5838}-1)}{0.85}}{\frac{1.5838-1}{1.5838} \times 0.7 \times 3.35 \times 0.85 + (1-0.7) \left[ 3.35-1 - \frac{\sqrt{1.5838}-1}{0.85} \right]} = 0.326$$

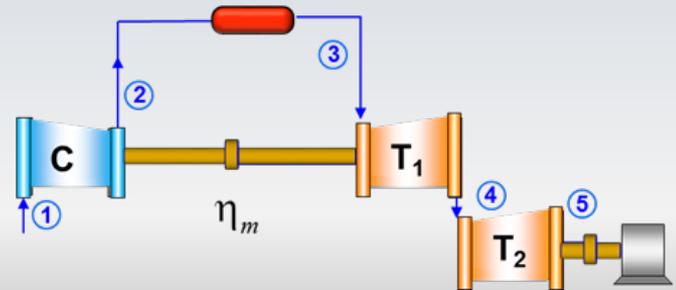


$$\eta = \frac{\frac{\Delta-1}{\Delta} \Phi \eta_T - \frac{2(\sqrt{\Delta}-1)}{\eta_c}}{\frac{\Delta-1}{\Delta} \sigma \Phi \eta_T + (1-\sigma) \left[ \Phi - 1 - \frac{\sqrt{\Delta}-1}{\eta_c} \right]}$$

# Problème

Les conditions pour l'installation ci-dessous sont les suivantes:  $p_{01}= 101.3 \text{ kPa}$  et  $T_{01}=288 \text{ K}$ . Le rapport de compression est  $r_c=9$ ,  $T_{03}=1380\text{K}$ ,  $\eta_C =0.87$ ,  $\eta_{T1} =0.89$ ,  $\eta_{T2}=0.89$ . Le pouvoir calorifique est  $\text{LHV}=43000\text{kJ/kg}$  et la pression à la sortie de la turbine de puissance  $T_2$  est  $p_{05}=120 \text{ kPa}$ . Considérez  $\eta_m =1$   $\gamma_c=1.4$  et  $\gamma_t=1.333$  et calculez:

- Le rapport débit massique de carburant /débit massique d'air:  $f$
- La température  $T_{05}$  à la sortie de la turbine de puissance ( $T_2$ )
- Le travail spécifique utile  $W_e$
- La rendement thermique du système  $\eta_{th}$



# Problème $f?$

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288\text{K}$ ,  $r_c = 9$ ,  $T_{03} = 1380\text{K}$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  
 $LHV = 43000\text{kJ/kg}$ ,  $p_{05} = 120 \text{ kPa}$ .  $\gamma_c = 1.4$ ,  $\gamma_t = 1.333$ ,  $\eta_m = 1$ ,  $c_{pt} = 1.148\text{kJ/kg}$ ,  $c_{pc} = 1.004\text{kJ/kg}$

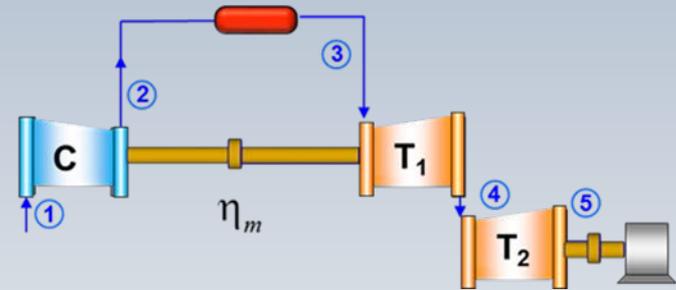
## Compresseur

$$p_{02} = r_c p_{01} = 9 \times 101.3 = \mathbf{911.7\text{kPa}}$$

$$T_{02} = T_{01} \left[ 1 + \frac{r_c^{(\gamma_c - 1)/\gamma_c} - 1}{\eta_c} \right]$$
$$= 288 \left[ 1 + \frac{9^{(1.4 - 1)/1.4} - 1}{0.87} \right] = \mathbf{577.53\text{K}}$$

## Chambre de combustion $f$

$$f = \frac{c_{p|t} T_{03} - c_{p|c} T_{02}}{LHV - c_{p|t} T_{03}} = \frac{1.148 \times 1380 - 1.004 \times 577.53}{43000 - 1.148 \times 1380} = \mathbf{0.0243}$$



# Problème

$T_{05}?$

$$f = 0.0243, \quad T_{02} = 577.53K$$

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288K$ ,  $r_c = 9$ ,  $T_{03} = 1380K$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  
 $LHV = 43000 \text{ kJ/kg}$ ,  $p_{05} = 120 \text{ kPa}$ .  $\gamma_c = 1.4$ ,  $\gamma_t = 1.333$ ,  $\eta_m = 1$ ,  $c_{pt} = 1.148 \text{ kJ/kg}$ ,  $c_{pc} = 1.004 \text{ kJ/kg}$

$$p_{03} = p_{02} = 911.7 \text{ kPa}$$

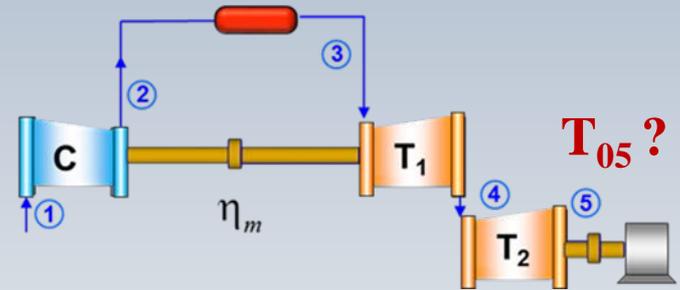
Turbine liée



$$T_{04} = T_{03} - \frac{1}{\eta_m(1+f)} \frac{c_{p|c}}{c_{p|t}} (T_{02} - T_{01})$$

$$= 1380 - \frac{1}{(1+0.0243)} \frac{1.004}{1.148} (577.53 - 288) = 1132.5K$$

$$p_{04} = p_{03} \left( 1 - \frac{T_{03} - T_{04}}{\eta_{T1} T_{03}} \right)^{\gamma_t / (\gamma_t - 1)} = 911.7 \left( 1 - \frac{1380 - 1132.5}{0.89 \times 1380} \right)^{1.333 / (0.333)} = 370.8 \text{ kPa}$$



# Problème

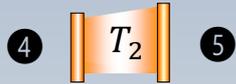
$$p_{04} = 370.8 \text{ kPa} \quad T_{04} = 1132.5 \text{ K} \quad f = 0.0243,$$

$$T_{05}? \quad W_e? \quad \eta_{th}?$$

$$p_{01} = 101.3 \text{ kPa}, \quad T_{01} = 288 \text{ K}, \quad r_c = 9, \quad T_{03} = 1380 \text{ K}, \quad \eta_C = 0.87, \quad \eta_{T1} = 0.89, \quad \eta_{T2} = 0.89,$$

$$\text{LHV} = 43000 \text{ kJ/kg}, \quad p_{05} = 120 \text{ kPa}. \quad \gamma_c = 1.4, \quad \gamma_t = 1.333, \quad \eta_m = 1$$

Turbine de puissance

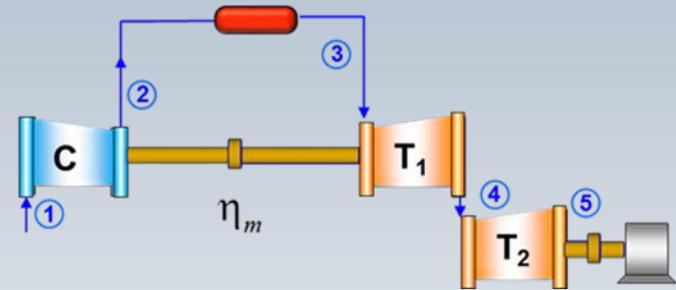


$$T_{05} = T_{04} \left[ 1 - \eta_{T2} \left( 1 - \left( \frac{p_{05}}{p_{04}} \right)^{(\gamma_t - 1)/\gamma_t} \right) \right]$$

$$= 1132.5 \left[ 1 - 0.89 \left( 1 - \left( \frac{120}{370.8} \right)^{(1.333 - 1)/1.333} \right) \right] = 884.8 \text{ K}$$

$$W_e = (1 + f) c_{pt} (T_{04} - T_{05})$$

$$= (1.0243) \times 1.148 (1132.5 - 884.8) = 292.27 \text{ kJ / kg}$$



$$\eta_{th} = \frac{W_e}{f \times \text{LHV}} \quad f = 0.0243$$

$$= \frac{292.27}{0.0243 \times 43000} = 0.279$$

# Problème: raccourci

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288 \text{ K}$ ,  $r_c = 9$ ,  $T_{03} = 1380 \text{ K}$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  
 $\text{LHV} = 43000 \text{ kJ/kg}$ ,  $p_{05} = 120 \text{ kPa}$ .  $\gamma_c = 1.4$ ,  $\gamma_t = 1.333$ ,  $\eta_m = 1$

$$\eta = \frac{\frac{\Delta - 1}{\Delta} \Phi \eta_T - \frac{2(\sqrt{\Delta} - 1)}{\eta_c}}{\frac{\Delta - 1}{\Delta} \sigma \Phi \eta_T + (1 - \sigma) \left[ \Phi - 1 - \frac{\sqrt{\Delta} - 1}{\eta_c} \right]}$$

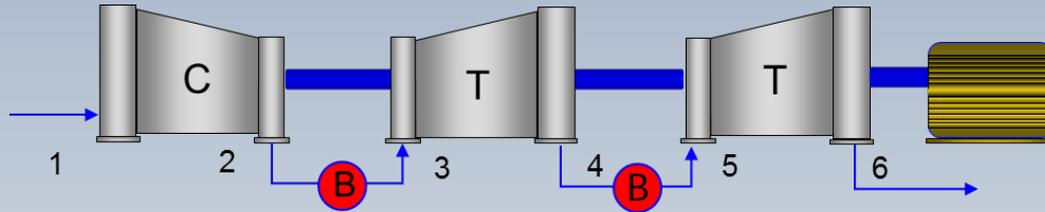
$$\Phi = \frac{T_{03}}{T_{02}} = 4.792$$

$$\Delta = \left( \frac{p_{02}}{p_{01}} \right)^{\gamma - 1 / \gamma} = 1.873$$

$$\sigma = 0$$

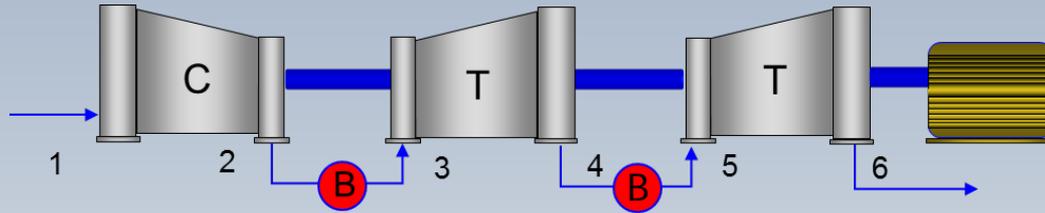
$$\eta = 0.339$$

# Problème



- La température et la pression à l'entrée du compresseur C sont  $T_{01} = 288 \text{ K}$  et  $p_{01} = 101.3 \text{ kPa}$
- Le rendement du compresseur (C)  $\eta_c = 87 \%$
- La pression à la sortie du compresseur  $p_{02} = 1216 \text{ kPa}$
- Le rendement des turbines  $\eta_t = 89 \%$
- La température à la sortie des chambres de combustion  $T_{03} = T_{05} = 1400 \text{ K}$
- Le pouvoir calorifique : LHV = 43000 kJ/kg

# Problème



Considérez  $c_p = \text{cnste}$  et calculez:

- Le travail de compression
- La pression  $p_{05} = p_{04}$
- La travail utile produit par la seconde turbine
- L'efficacité thermique
- La consommation spécifique

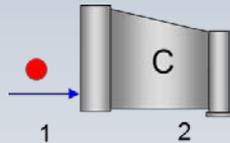
# Problème

$w_c?$

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288 \text{ K}$ ,  $T_{03} = 1400 \text{ K}$ ,  $\eta_c = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $p_{02} = 1216 \text{ kPa}$ .  $\gamma_c = 1.4$ ,  $\eta_m = 1$ ,  $c_p = 1.004 \text{ kJ/kg-K}$

Entrée du compresseur :

$$T_{01} = 288 \text{ K}$$



$$\frac{T_{02s}}{T_{01}} = \left( \frac{p_{02}}{p_{01}} \right)^{\frac{\gamma-1}{\gamma}}$$

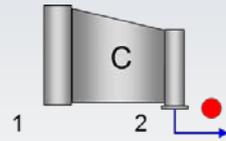
" Pont isentropique "



$$= (r_p)^{\frac{\gamma-1}{\gamma}} = (12)^{0.2857}$$

Sortie du compresseur

$$T_{02} = T_{01} + \frac{T_{02s} - T_{01}}{\eta_c} = 630.3 \text{ K}$$



$$T_{02s} = 585.8 \text{ K}$$

$$T_{02} = 630.3 \text{ K}$$

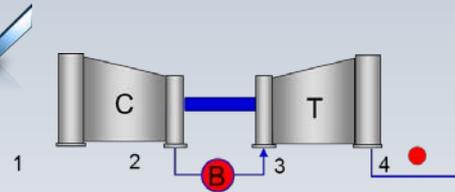
# Problème

$w_c?$

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288\text{K}$ ,  $T_{03} = 1400\text{K}$ ,  $\eta_c = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  $\text{LHV} = 43000\text{kJ/kg}$ ,  
 $p_{02} = 1216 \text{ kPa}$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $c_p = 1.004 \text{ kJ/kg-K}$

$$w_{cs} = c_p(T_{02s} - T_{01}) = 1.0045(585.8 - 288) = 299.1 \text{ kJ/kg}$$

$$w_{cr} = \frac{w_{cs}}{\eta_c} = \frac{299.1}{0.87} = 343.83 \text{ kJ/kg}$$



$$w_{tr} = w_{cr} = 343.83 \text{ kJ/kg}$$

“ Pont isentropique ”

$$w_{ts} = \frac{w_{tr}}{\eta_t} = \frac{343.83}{0.89} = 386.34 \text{ kJ/kg}$$



# Problème

$p_{04}?$

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288 \text{ K}$ ,  $T_{03} = 1400 \text{ K}$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $p_{02} = 1216 \text{ kPa}$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $c_p = 1.004 \text{ kJ/kg-K}$

$$T_{03} = 1400 \text{ K}$$



Processus isentropique 3-4

$$w_{ts} = 386.34 \text{ kJ/kg}$$

$$T_{04s} = T_{03} - \frac{w_{ts}}{c_p} = 1015.4 \text{ K}$$

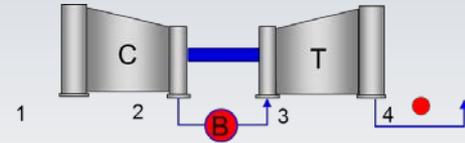
$$w_{tr} = 343.83 \text{ kJ/kg}$$

Processus réel 3-4

$$T_{04} = T_{03} - \frac{w_{tr}}{c_p} = 1057.7 \text{ K}$$

$$\frac{p_{04}}{p_{03}} = \left( \frac{T_{04s}}{T_{03}} \right)^{\gamma/\gamma-1}$$

$$p_{04} = 395.8 \text{ kPa} \quad (p_{03} = p_{02})$$



# Problème

$w_{t2r}$ ?

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288 \text{ K}$ ,  $T_{03} = 1400 \text{ K}$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $p_{02} = 1216 \text{ kPa}$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $c_p = 1.004 \text{ kJ/kg-K}$

$$p_{04} = p_{05} = 395.82 \text{ kPa}$$

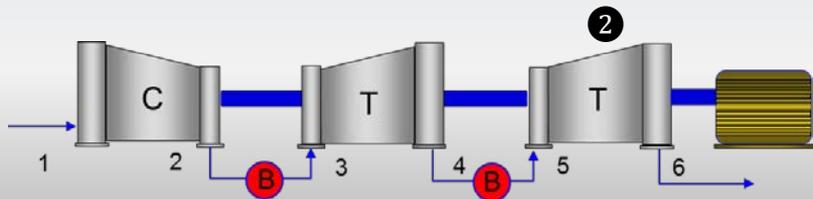
$$p_{06} = p_{01} = 101.3 \text{ kPa}$$

$$T_{03} = T_{05} = 1400 \text{ K}$$

$$\frac{p_{06}}{p_{05}} = \left( \frac{T_{06s}}{T_{05}} \right)^{\gamma/\gamma-1} \Rightarrow T_{06s} = 948.5 \text{ K}$$

Processus 5-6

$$w_{t2r} = c_p (T_{05} - T_{06s}) \eta_t = 403.7 \text{ kJ/kg}$$



# Problème

$p_{01} = 101.3 \text{ kPa}$ ,  $T_{01} = 288\text{K}$ ,  $T_{03} = 1400\text{K}$ ,  $\eta_C = 0.87$ ,  $\eta_{T1} = 0.89$ ,  $\eta_{T2} = 0.89$ ,  $LHV = 43000\text{kJ/kg}$ ,  
 $p_{02} = 1216 \text{ kPa}$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $c_p = 1.004 \text{ kJ/kg-K}$

**Efficacité thermique**

$$w_{t2r} = 403.7 \text{ kJ/kg}$$

$$T_{03} = 1400 \text{ K}$$

$$T_{02} = 630.3\text{K}$$

$$T_{04} = 1057.1\text{K}$$

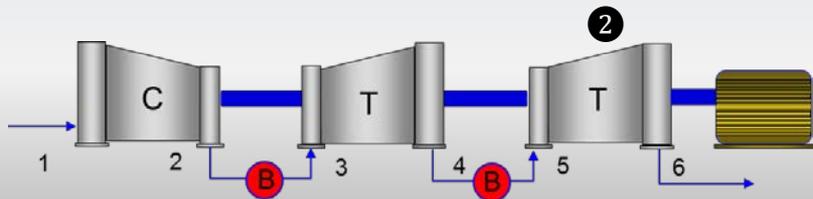
$$T_{05} = 1400\text{K}$$

$$q_{c.c} = c_p \left[ (T_{05} - T_{04}) + (T_{03} - T_{02}) \right] = 1159.5 \text{ kJ/kg}$$

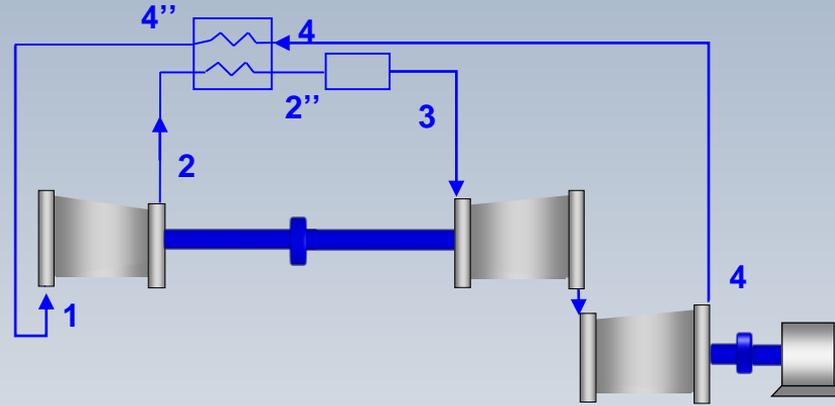
$$\eta_{th} = \frac{w_{t2r}}{q_{c.c}} = \frac{403.7}{1159.5} = 0.348$$

$$SFC = \frac{3600}{\eta_{th} \times LHV}$$

$$= \frac{3600}{0.348 \times 43000} = 0.24 \frac{\text{kJ}}{\text{kWh}}$$

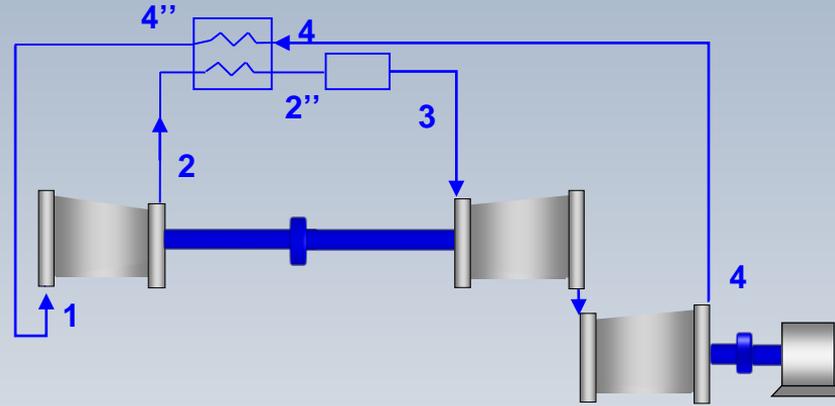


# Problème



Les conditions pour ce cycle régénératif sont les suivantes:  $p_{01} = p_{04} = 8 \text{ bar}$  et  $T_1 = 30^\circ\text{C}$ . Le rapport de compression est  $r_c = 4$ ,  $T_3 = 850^\circ\text{C}$ ,  $\eta_c = 0.85 = \eta_T$ ,  $\sigma = 0.7$ , et le débit massique  $\dot{m} = 30 \text{ kg/s}$ . Considérez  $c_p = \text{cnste}$  (air) et calculez:

# Problème $c_p = \text{cnste}$



- La température à la sortie de la turbine de puissance ( $T$  libre)
- La température à l'entrée de la chambre de combustion  $T_{2''}$ .
- La température à l'entrée du régénérateur  $T_2$
- La température à la sortie du régénérateur  $T_{4''}$
- La puissance consommée par le compresseur
- La puissance générée par les turbines

# Problème

$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30 \text{ }^\circ\text{C}$ ,  $T_{03} = 850 \text{ }^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

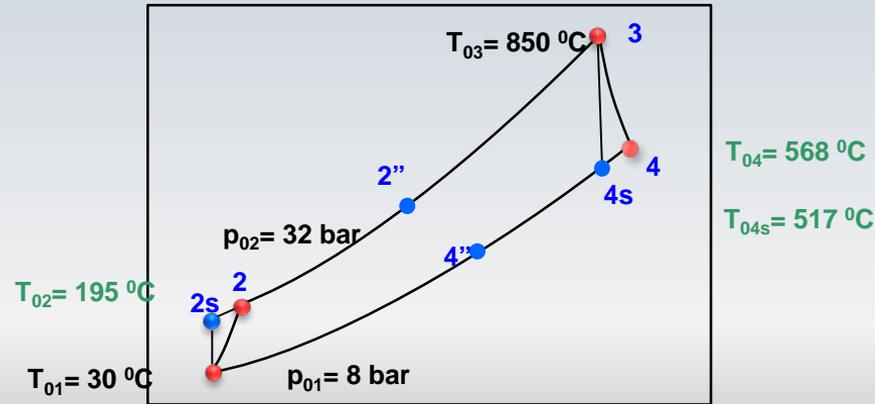
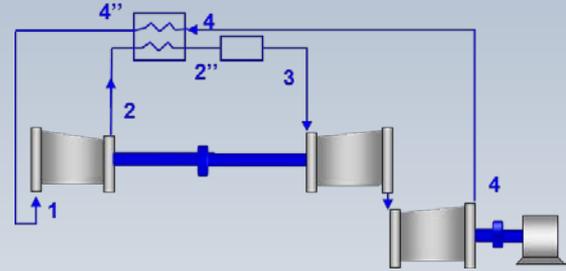
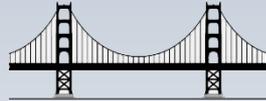
$$T_{01} = 303 \text{ K}$$

$$\frac{T_{02s}}{T_{01}} = \left( \frac{p_{02}}{p_{01}} \right)^{\frac{\gamma-1}{\gamma}}$$

$$= (r_p)^{\frac{\gamma-1}{\gamma}} = (4)^{0.2857}$$

$$T_{02s} = 450.2 \text{ K}$$

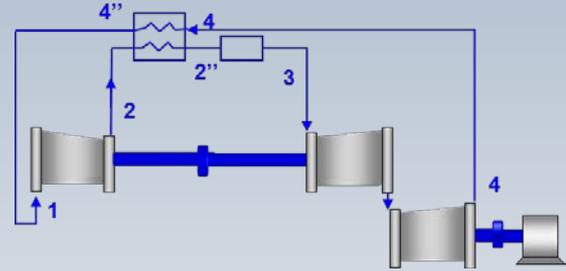
" Pont isentropique "



# Problème

$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30 \text{ }^\circ\text{C}$ ,  $T_{03} = 850 \text{ }^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

$$T_{02} = T_{01} + \frac{T_{02s} - T_{01}}{\eta_c} = 303 + \frac{450.2 - 303}{0.85} = 476.2 \text{ K}$$



$$T_{03} = 1123 \text{ K} \rightarrow$$

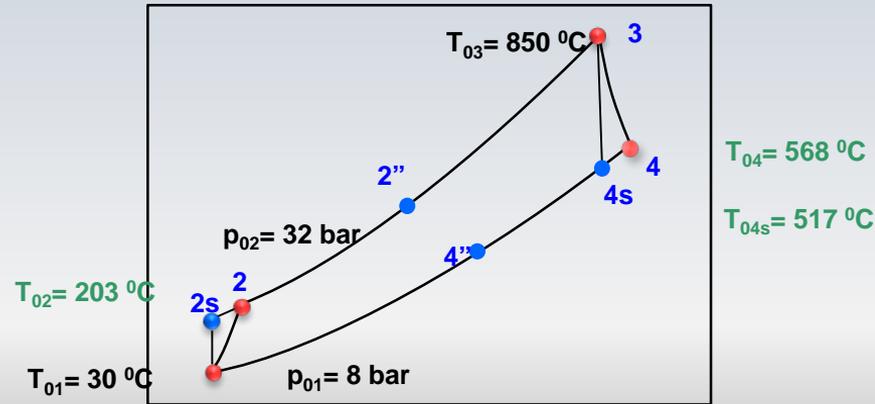
" Pont isentropique "



$$\frac{p_{04}}{p_{03}} = \left( \frac{T_{04s}}{T_{03}} \right)^{\gamma/\gamma-1}$$

$$\frac{1}{4} = \left( \frac{T_{04s}}{1123} \right)^{\gamma/\gamma-1}$$

$$T_{04s} = 755.7 \text{ K}$$



# Problème

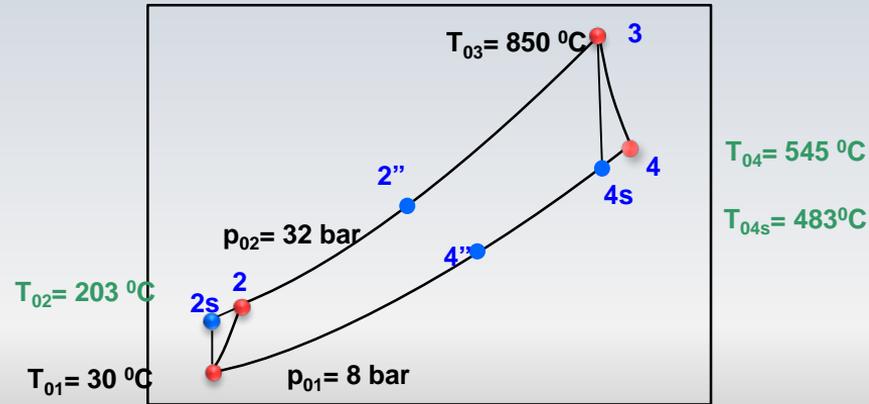
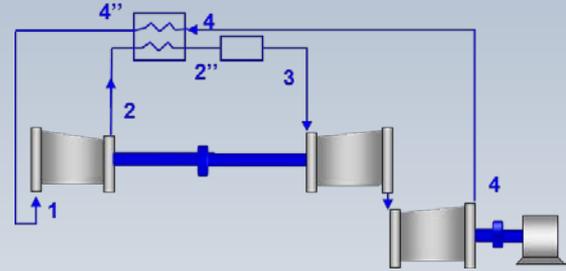
$p_{01} = p_{04} = 8 \text{ bar}$     $T_{01} = 30 \text{ }^\circ\text{C}$ ,    $T_{03} = 850 \text{ }^\circ\text{C}$ ,    $r_C = 4$ ,    $\eta_C = 0.85$ ,    $\eta_T = 0.85$ ,    $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .    $\gamma_c = 1.4$     $\eta_m = 1$ ,    $\dot{m} = 30 \text{ kg/s}$

→  $T_{04s} = 755.7 \text{ K}$  •

$$T_{04} = T_{03} - \eta_T(T_{03} - T_{04s})$$

$$T_{04} = 1123 - 0.85(1123 - 755.7) = 817.7 \text{ K}$$

•  $T_{04} = 817.7 \text{ K}$  ✓



# Problème

$$T_{04} = 817.7 K$$

$$T_{02} = 476.2 K$$

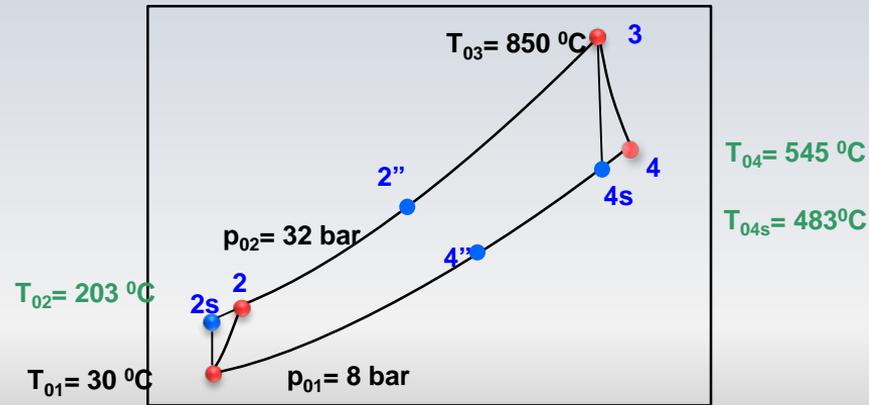
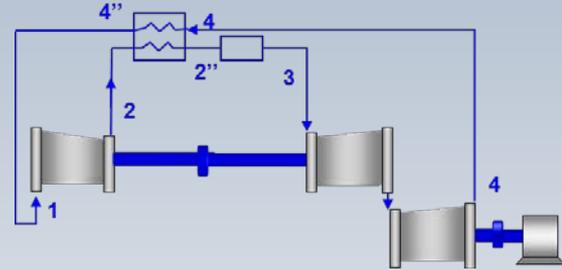
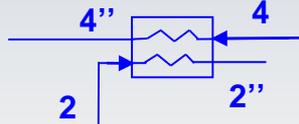
$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30 \text{ }^\circ\text{C}$ ,  $T_{03} = 850 \text{ }^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

$$\sigma = \frac{T_{02}'' - T_{02}}{T_{04} - T_{02}} = 0.7 \quad T_{02}'' = T_{02} + \sigma(T_{04} - T_{02})$$

$$T_{02}'' = 476.2 + 0.7(817.7 - 476.2) = 715.2 K$$

$$T_{02}'' - T_{02} = T_{04} - T_{04}''$$

$$T_{04}'' = T_{04} + T_{02} - T_{02}''$$



# Problème

$$\rightarrow T_{02}'' = 715.2K \quad T_{02} = 476.2K \quad T_{04} = 817.7K \quad T_{01} = 303K$$

$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30 \text{ }^\circ\text{C}$ ,  $T_{03} = 850 \text{ }^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

$$T_{04} \quad T_{02} \quad T_{02}''$$

$$T_{04}'' = 817.7 + 476.2 - 715.2 = 578.6K$$

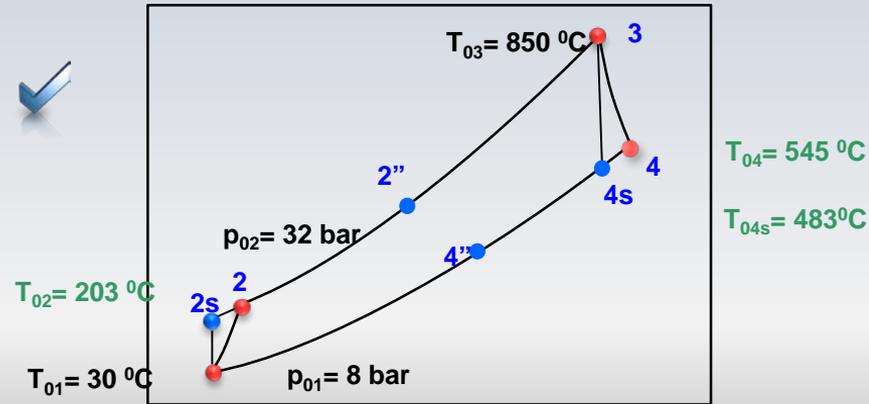
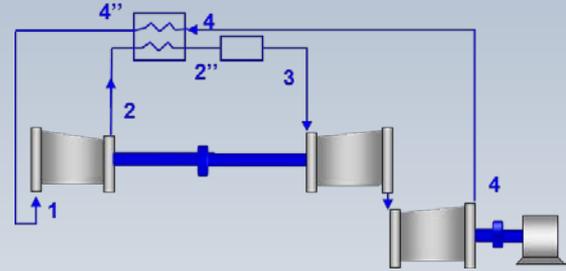
$$\rightarrow T_{04}'' = 578.6K$$

$$\dot{W}_c = \dot{m} c_p (T_{02} - T_{01}) = 30 \times 1.004 (476.2 - 303)$$

$$\dot{W}_c = 5216.8 \text{ kW}$$

$$\dot{W}_t = \dot{m} c_p (T_{03} - T_{04}) = 30 \times 1.004 (1123 - 817.7)$$

$$= 9196 \text{ kW}$$



# Problème

$$\rightarrow T_{02}'' = 714.2K \quad T_{02} = 476.2K \quad T_{04} = 867.1K \quad T_{01} = 303K$$

$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30 \text{ }^\circ\text{C}$ ,  $T_{03} = 850 \text{ }^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

$$\dot{W}_t = 9196 \text{ kW} \quad \dot{W}_c = 5216 \text{ kW}$$

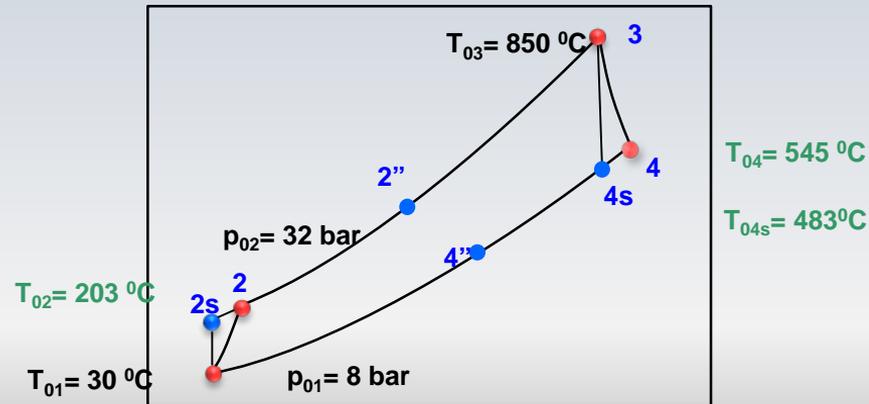
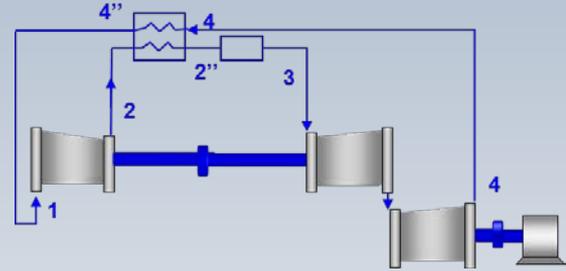
$$W_e = (\dot{W}_t - \dot{W}_c) / \dot{m} = 132.7 \text{ kJ / kg}$$



$$T_{03} = 1123K \quad T_{02}'' = 715.2K$$

$$q = c_p (T_{03} - T_{02}'') = 407.8 \text{ kJ / kg}$$

$$\eta = \frac{W_e}{q} = \frac{132.7}{407.8} = 0.32$$



# Problème

$$\rightarrow T_{02}'' = 714.2K \quad T_{02} = 476.2K \quad T_{04} = 867.1K \quad T_{01} = 303K$$

$p_{01} = p_{04} = 8 \text{ bar}$   $T_{01} = 30^\circ\text{C}$ ,  $T_{03} = 850^\circ\text{C}$ ,  $r_c = 4$ ,  $\eta_c = 0.85$ ,  $\eta_T = 0.85$ ,  $\text{LHV} = 43000 \text{ kJ/kg}$ ,  
 $\sigma = 0.7$ .  $\gamma_c = 1.4$   $\eta_m = 1$ ,  $\dot{m} = 30 \text{ kg/s}$

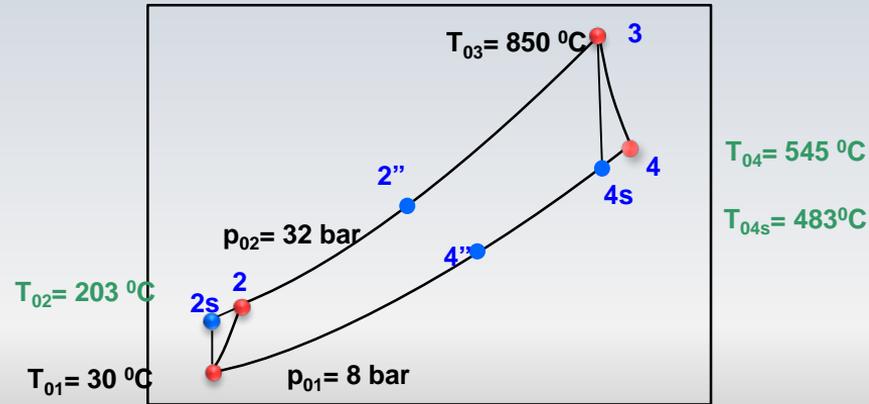
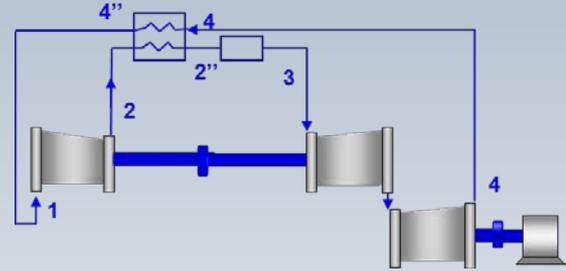
$$\Delta = 4^{\frac{\gamma-1}{\gamma}} = 1.4886$$

$$\Phi = \frac{T_3}{T_1} = \frac{1123}{303} = 3.706$$

$$c_p = 1.004 \text{ kJ/kg.K}$$

$$W_e = c_p T_1 \left( \frac{\Delta - 1}{\Delta} \right) \left( \eta_T \Phi - \frac{\Delta}{\eta_c} \right)$$

$$= 139.88 \text{ kJ/kg.K}$$



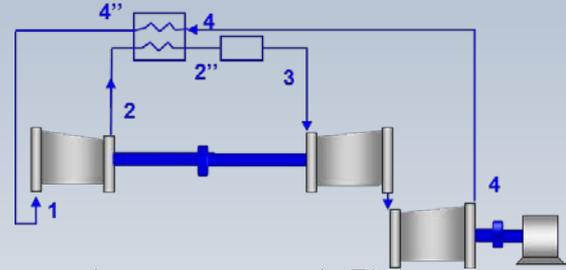
# Problème

$$\rightarrow T_{02}'' = 714.2K \quad T_{02} = 476.2K \quad T_{04} = 867.1K \quad T_{01} = 303K$$

$$p_{01} = p_{04} = 8 \text{ bar} \quad T_{01} = 30 \text{ }^\circ\text{C}, \quad T_{03} = 850 \text{ }^\circ\text{C}, \quad r_c = 4, \quad \eta_c = 0.85, \quad \eta_T = 0.85, \quad \text{LHV} = 43000 \text{ kJ/kg}, \\ \sigma = 0.7, \quad \gamma_c = 1.4 \quad \eta_m = 1, \quad \dot{m} = 30 \text{ kg/s}$$

$$\Delta = 1.4886 \quad \Phi = 3.706 \quad c_p = 1.004 \text{ kJ/kg}\cdot\text{K}$$

$$W_e = 139.88 \text{ kJ/kg}\cdot\text{K}$$



$$Q = c_p T_1 \left( \Phi - \left\{ \left( 1 + \frac{\Delta - 1}{\eta_c} \right) + \sigma \left[ \Phi \left( 1 - \eta_T \frac{\Delta - 1}{\Delta} \right) - \left( 1 + \frac{\Delta - 1}{\eta_c} \right) \right] \right\} \right)$$

$$Q = 411.81 \text{ kJ/kg}$$

$$\eta = \frac{W_e}{q} = \frac{139.88}{411.81} = 0.34$$

